

HONORS

2024-02-21

1

ALGORITHMS

Predicates on a set A

$$f: A \rightarrow \{0, 1\}$$

No YES
FALSE TRUE

1-to-1 corr. to subsets: $B \subseteq A$

$$f_B(a) = \begin{cases} 1 & \text{if } a \in B \\ 0 & \text{if } a \in A \setminus B \end{cases}$$

$$B \mapsto f_B$$

Σ finite set "alphabet"

e.g. $\Sigma = \{0, 1\}$ binary alphabet

→ $\Sigma = \{\{, \}, (,), \text{comma}, 0, 1\}$

Graph: edge-list rep $\{\{1, 2, 3, \dots, n\}, \{1, 2\}, \{2, 3\}, \dots\}$

adjacency
matrix

0111010101...

n^2

⊕ $(n+m) \cdot \log n$

Σ alphabet

3

Σ^n : set strings of length n
words over Σ

$a_1 \dots a_n \in \Sigma^n$ if $a_i \in \Sigma$

$$\Sigma^* = \bigcup_{n=0}^{\infty} \Sigma^n$$

empty string Λ

all $\uparrow$ strings

LANGUAGE $L \subset \Sigma^*$

PRIME = {prime numbers in binary}

COMPOSITE = { $n \geq 2$ / n not prime}

GRAPHS

3COL = {3-colorable graphs}

HAM = {Hamiltonian graphs}

L has Hamilton cycle
(passes through
every vertex)

$$\text{CLIQUE} = \{ (G, k) \mid G \text{ graph} \\ k \in \mathbb{N} \}$$

$$\omega(G) \geq k \}$$

clique number

G has a clique of size k

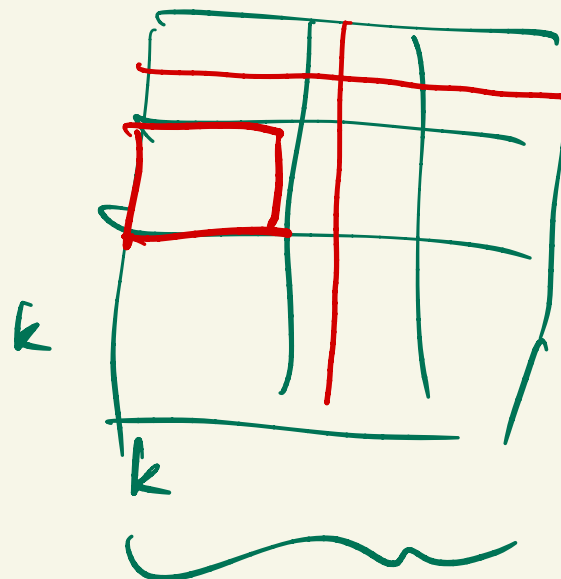
SUDOKU

entries

$0, 1, \dots, k^2$



blank



feasible: $\exists$ solution k

(6)

P : set of languages recognizable
in polynomial time

corresponding predicate

computable in poly. time

membership testing

Class : set of sets

Complexity class: set of languages

P is a complexity class