# Enigma <br> CMSC 28400, Autumn 2021, Lecture 2 

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## Enigma

Reflector (Umkehrwalze, not visible)

Three rotors
(Walzen)

Lightboard (output)

Keyboard


Plugboard
(Steckerbrett)






## 1930s Enigma Setup (Changes each day)

1. Pick three rotors to use
2. Pick order for three rotors
3. Pick ring setting (rotate casing; changes turnovers)
4. Pick three initial rotor positions
5. Pick plugboard connections

für Oktpber 1944

|  | Datum： | Wabealage |  |  | Ringstelliang |  |  | Steckerverbindungen |  |  |  |  |  |  |  |  |  | herngruppen |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5. | 31. | IV | V | I | 21 | 15 | 16 | KL | I＇T | FQ | HY | RG． | NP | $V 2$ | JB | SE | OG | ．jkg | ORI | ncj | $g 1 p$ |
| St | 30. | IV | II | III | 20 | 14 | 11 | － $\mathrm{Z} \mathrm{N}^{*}$ | 10 | GB | ER | DK | XU | GF | TV | S J | LM | ino | ud 1 | nam | $\operatorname{lax}$ |
| St | 29. | IT． | 7 | IV | 19 | 09 | 24 | 2 J | HL | CQ | \％M | OA | PY | EB | TR | DN | VI | nc 1 | oid | yhp | ก1p |
| St | 28. | （IV | III | I | 03 | 04 | 22 | YT | BX | CV | 2 N | UD | IR | 5.1 | 116 | 3A | Ke | zqJ | h7 g | xky | ebt |
| St． | 27. | V | I | IV | 20 | 0 C | 18 | KX | GJ | EP | AC | TH | HL | MW | QS | DV | 02 | bvo | sur | Ucc | lqe |
| St | 26. | IV | I | V | 10 | 17 | 1） | Y V | GT | OQ1 | WN | FI | SK | L． D | RP | MZ | 30 | jhx | u14h | giw | ugw |
| $3 t$ | 25. | V | IV | III | 13 | 04 | 17 | QR | GE | HA | NM | $\checkmark 5$ | WD | YZ | OF | XK | PE | tba | pnc | ukd | n 1 d |
| St | 24. | IIT | II | IV | 09 | 2） | 18 | HS | NC | WK | GO | YQ | AX | EH | V J | 2L | PF | n土i | mew | xbk | yes |
| St | 23. | V | IT | HI | 11 | 21 | 08 | EY | DT | KF | MO | A ${ }^{\text {P }}$ | HN | \％ 6 | ZL | TV | JA | 1sd | nuo | YCr | vox |
| St | 22. | $I$ | II | IV | 01 | 25 | 02 | PZ | SE | 0 J | あ | HA | GB | $V Q$ | UY | KW | EF | Y． 11 | rwy | rdk | nso |
| St | 21. | IV． | I | III | 116 | 22 | 03 | GH | JR | TQ | KF | N2 | IL | WM | BD | 00 | EO | ema | mly | j． y | iqh |
| S $\pm$ | 20. | V | I | II | 12 | 25 | 08 | TP | K8 | XV | リZ | $P Y$ | NL， | W I | S．J | ME | GB4 | $\times 11$ | pgs | geh | znd |
| St | 19. | IV | III | II＇ | 07 | 05 | 23 | 2 8 | EU | AC | GD | KP | VO | QS | NW | HL | B，M | vpj | \％qe | jr＇s | egm |
| St | 18. | II | IIT | Y | 19 | 14 | $\underline{2}$ | WG | OH． | RL | DR． | 89． | 49 | P－7 | \％ 8 | Y赶 | IJ | $0 \times$ | 1eb | \％d | dy ${ }^{\text {c }}$ |
| St | 17. | IV | I | II | 12 | 0 N | 21 | ME | HX | EF | VY | 2D | TR | ［J | AG | IL | KQ | tak | pje | kdh | jvh |
| St | 16. | I | II | III | 07 | 11 | 15 | W2 | AB | MO | $\mathrm{F}_{\mathrm{F}} \mathrm{F}$ | RX | SG | QU | \％ | YN | EL | pz | evw | Wyt | iye |
| St | 15. | III | II | $V$ | 00 | 16 | 02 | GT | YC | EJ | IA | RX | FN | 15 | WB | MH | 2 V | bhe | x 2 II | $y \mathrm{zk}$ | evp |
| St | 14. | II | I |  | 23 | 05 | 24 | A 2 | CJ | WF | dy | SO | QV | M I | NH | DP | GX | $f d x$ | ty．j | bmq | typ |
| $\stackrel{\text { t }}{ }$ | 13. | IV | He |  | 03 | 2.5 | 10 | CK | KN | $J R$ | DQ | 10 | TL | Hz | MF | EP | WB | zf | bir | ZW太 | g＊i |
| St | 12. | I | III | II | 20 | 01 | 18 | QB | YE | WN | A1 | OJ | TO | HR | PK | PS | CM | UPO | aut | tkr | pw\％ |
| St | 11. | V |  |  | 17 | 1.4 | 12.4 | SV | GO | PA | 2 R | PN | HI | YK | WT | DE | B． 3 | $v \mathrm{dr}$ | ego | wmy | uti |
| St | 10. | I | V | IV | 26 | 07 | 16 | SW－ | AQ | NE | For | WY | UX | MK | CL | HT | 2.1 | r | ลาฟ | vpr | mhr |
| St | 9. | I | III |  | 17 | 10 | 18 | B． | IR | GK | NZ | SP | UA | LD | CQ | JM | YV | kno | $y s q$ | rhj | t1．j |
| St | 8. | ，V | ．II | I | 23 | 11 | 25 | QY | OG | ST | HA | CE | WD | KL | JN | VK | IU | 150 | avx． | $\mathbf{a x h}$ | 自W ${ }^{\text {j }}$ |
| St | 7. | II | III | I | 06 | 12 | 03 | BG | FS | TH | JE | VK | P＇E | CU | QA | OD | NM | aty | mbb | mvo | $j \mathrm{mz}$ |
| St | 6. | I | IV | $V$ | 24 | 19 | 01 | IR | HQ | NT | WZ | VC | OY | GP | －LF | BX | AK | bho | 1W0 | 2 gz | rnr |
| St | 5. | II | 4V | HI | 05 | 22 | 14 | MK | 00 | FQ | XT | DW | IA | ZI， | SY | PJ | EF＊ | bo | rzw | $\mathrm{kz} \mathrm{O}^{+}$ | ry1 |
| St | 4. | IV |  | I | 15 | 02 | 21 | KD | PG | CO | FW | HJ | RY | MT | QL | VB | 0 O | kpk | php | $x \mathrm{mo}$ | pfit |
| St | 3. | III | V |  | 03 | 27 | 0.4 | DY | CF | WN | OV | 9 H | 1\％ | RA | TI | GL， | SM | h．jy | nkt | $y \mathrm{tn}$ | pvo |
| St | 2. | I | III |  | 13 | 15 | 01 | DR | V．J | FS | \％ | IU | HX | A9 | GT | YO | FC | $p \mathrm{pq}$ | 19＊ | oiy | ru， |
| Et | 1. | II | IV |  | 06 | 17 | 26 | AS | LS | BQ | WN | MY | UV | FJ | $\mathrm{P} \mathbf{8}$ | TR | OK | 0 O | 001 | yw | fo |

## Basic Enigma Usage: Encryption

1. Setup from key instructions
2. Type a letter
3. Board lights up with output letter, rotors move 4. Goto 2

## Basic Enigma Usage: Decryption - The same!

1. Setup from key instructions
2. Type a letter
3. Board lights up with output letter, rotors move
4. Goto 2


## Enigma Randomization: Message Keys

Problem: All senders would apply same permutation to first character, then same to second etc.


Solution: Use "message keys" that randomize the initial rotor positions for each message:

1. Setup from key instructions
2. Pick a random rotor position (say RTP)
3. Encrypt and send RTPRTP
4. Reset rotor positions to RTP
5. Send message as before

## Today and Tomorrow: Rejewski's Attack

Polish Cipher Bureau achieved a complete break of this version of Enigma!

## We will assume:

1. We have captured many ciphertexts encrypted with the same day settings
2. We don't know any of the rotor wirings or day key settings

Our Goal: Recover message keys efficiently

We will only do one part of the attack; The entire attack involves many tedious steps.

The End

